Which Bulb Burns Brighter?

One is a 60-watt bulb and the other a 100-watt bulb, and they are connected in an electric circuit.

Look at the text on page 541 for the answer.
Your desk needs to be well lit. You have a 100-watt lightbulb and a 60-watt lightbulb available for your desk lamp. Which of the two lightbulbs would you choose? You know a watt is a unit of power, so you might expect that a 100-watt lightbulb would always produce more light than a 60-watt bulb. But would it?

You’re shopping for a string of holiday lights for a party. You find a string of pumpkin lights with a tag that reads “If one goes out, the rest stay lit.” Why is this important? How are the lights connected to each other and the power source to make sure that the rest stay lit?

Does the type of electric circuit that connects the bulb make a difference? Suppose the lightbulbs are in a circuit unlike the parallel circuit that normally connects lightbulbs in your home. For example, in the photo at the left, the bulbs are connected in series. Does that make a difference? Can you figure out why? To answer these questions, you need to know how a series circuit differs from a parallel circuit.

In Chapter 22, you studied circuits that had one source of electric energy, for example, a battery and one device such as a motor or a lamp that converted the electric energy to another form. But circuits can be much more versatile than that. In this chapter, you’ll explore several ways in which devices may be connected in electric circuits. By the end of this chapter, you’ll have no trouble deciding which of the two bulbs at the left is brighter and why the rest of the bulbs stay lit.
OBJECTIVES

- **Describe** both a series connection and a parallel connection and **state** the important characteristics of each.
- **Calculate** current, voltage drops, and equivalent resistance for devices connected in series and in parallel.
- **Describe** a voltage divider and **solve** problems involving one.

**FIGURE 23–1** No matter what path the water of a river takes down a mountain, the amount of water and the drop in elevation are the same.

**23.1 Simple Circuits**

If you have ever had the chance to explore rivers in the mountains, such as the river shown below in **Figure 23–1**, the following description will be familiar. From their sources high in the mountains, rivers make their way to the plains below. No matter what path they take, the change in elevation, from the mountaintop to the plain, is the same. Some rivers flow in a single stream, tumbling through a series of rapids and over waterfalls. Other rivers split into two or more streams as they flow over a waterfall or through the rapids. Part of the river follows one path; other parts find different routes. But no matter how many paths the water takes, the total amount of water flowing down the mountain is the same, and the vertical drop from mountaintop to plain is the same distance.

Mountain rivers can serve as a model for electric circuits. The distance the water drops is similar to potential difference. The amount of water flowing through the river each second is similar to current. Narrow rapids are like a large resistance. But what is similar to a battery or generator? Just as in an electrical circuit, an energy source is needed to raise water to the top of the mountain. As you learned in Earth science, the source of energy is the sun. Solar energy evaporates water from lakes and seas and forms clouds that release rain or snow to fall on the tops of mountains. Think about the mountain river model as you read about the current in electrical circuits.
Series Circuits

Pat, Chris, and Ali were connecting two identical lamps to a battery as illustrated in Figure 23–2. Before making the final connection to the battery, their teacher asked them to predict the brightness of the two lamps. They knew that the brightness of a lamp depends on the current flowing through it. Pat said that only the lamp closer to the + terminal of the battery would light because all the current would be converted into light. Chris said that the second lamp would light, but it would be dimmer than the other one because some electrical energy would be changed into thermal and light energy. Consequently, there would be less electrical energy left for the second lamp. Ali said that both lamps would be equally bright because current is a flow of charge, and because the charge leaving the first lamp had nowhere else to go in the circuit except through the second lamp, the current would be the same in the two lamps. Who do you think is right?

If you consider the mountain river model for this circuit, you’ll see that Ali is correct. Charge has only one path to follow. Recall from Chapter 20 that charge cannot be created or destroyed, so the same amount of charge must leave a circuit as enters the circuit. This means that the current is the same everywhere in the circuit. If you connect three ammeters into a circuit as shown in Figure 23–3, they all have the same value. A circuit such as this, in which all current travels through each device, is called a series circuit.

But how could you answer Chris? If the current is the same, what changes in the lamp to produce the thermal and light energy? Recall that power, the rate at which electrical energy is converted, is represented by \( P = IV \). Thus, if there is a potential difference or voltage drop across the lamp, then electrical energy is being converted into another form. The resistance of the lamp is defined as \( R = \frac{V}{I} \). Thus, the potential difference, also called the voltage drop, is \( V = IR \).

**What is the current in the series circuit?** From the river model, you know that the sum of the drops in height at each rapid is equal to the total drop from the top of the mountain to sea level. In the electrical circuit, the increase in voltage provided by the generator or other energy source, \( V_{\text{source}} \), is equal to the sum of voltage drops across the lamps A and B.

\[
V_{\text{source}} = V_A + V_B
\]

Because the current, \( I \), through the lamps is the same, \( V_A = IR_A \) and \( V_B = IR_B \). Therefore, \( V_{\text{source}} = IR_A + IR_B \) or \( V_{\text{source}} = I(R_A + R_B) \).

The current through the circuit is represented by the following.

\[
I = \frac{V_{\text{source}}}{R_A + R_B}
\]

This equation applies to any number of resistances in series, not just two. The same current would exist with a single resistor, \( R \), that has a
Resistance equal to the sum of the resistances of the two lamps. Such a resistance is called the equivalent resistance of the circuit. For resistors in series, the **equivalent resistance** is the sum of all the individual resistances.

**Equivalent Resistance for Resistors in Series**

\[
R = R_A + R_B + \ldots
\]

Notice that the equivalent resistance is larger than any single resistance. Therefore, if the battery voltage doesn’t change, adding more devices in series always decreases the current. To find the current, \( I \), through a series circuit, first calculate the equivalent resistance, \( R \), and then use the following equation to calculate \( I \).

\[
I = \frac{V_{\text{source}}}{R}
\]

**Practice Problems**

1. Three 20-\( \Omega \) resistors are connected in series across a 120-V generator. What is the equivalent resistance of the circuit? What is the current in the circuit?

2. A 10-\( \Omega \) resistor, a 15-\( \Omega \) resistor, and a 5-\( \Omega \) resistor are connected in series across a 90-V battery. What is the equivalent resistance of the circuit? What is the current in the circuit?

3. Consider a 9-V battery in a circuit with three resistors connected in series.
   a. If the resistance of one of the resistors increases, how will the series resistance change?
   b. What will happen to the current?
   c. Will there be any change in the battery voltage?

4. A string of holiday lights has ten bulbs with equal resistances connected in series. When the string of lights is connected to a 120-V outlet, the current through the bulbs is 0.06 A.
   a. What is the equivalent resistance of the circuit?
   b. What is the resistance of each bulb?

5. Calculate the voltage drops across the three resistors in problem 2, and check to see that their sum equals the voltage of the battery.

**Pocket Lab: Series Resistance**

Hook up a power supply, a resistor, and an ammeter in a series circuit. Predict what will happen to the current in the circuit when a second, identical resistor is added in series to the circuit. Predict the new currents when the circuit contains three and four resistors in series. Explain your prediction. Try it.

**Analyze and Conclude** Make a data table to show your results. Briefly explain your results. (Hint: Include the idea of resistance.)

**Voltage drops in a series circuit** In any circuit, the net change in potential as current moves through it must be zero. This is because the electrical energy source in the circuit, the battery or generator, raises the potential. As current passes through the resistors, the potential drops an amount equal to the increase, and, therefore, the net change is zero.

The potential drop across each resistor in a series circuit can be calculated by rearranging the equation that defines resistance, \( R = V/I \), to
solve for \( V \), \( V = IR \). First, find the equivalent resistance, \( R \), in the circuit by calculating the sum of all the individual resistances. Then, to find the current, which is the same everywhere in the circuit, use the equivalent resistance and the equation \( I = \frac{V}{R} \), where \( V \) is the potential drop. Having determined the current in the circuit, multiply \( I \) by the resistance of the individual resistor to find the potential drop across that resistor.

An important application of series resistors is the voltage divider. A **voltage divider** is a series circuit used to produce a voltage source of desired magnitude from a higher-voltage battery. Suppose you have a 9-V battery but need a 5-V potential source. A voltage divider can supply this voltage. Consider the circuit shown in **Figure 23–4**. Two resistors, \( R_A \) and \( R_B \), are connected in series across a battery of magnitude \( V \). The equivalent resistance of the circuit is \( R = \frac{R_A R_B}{R_A + R_B} \). The current, \( I \), is represented by the following equation.

\[
I = \frac{V}{R} = \frac{V}{R_A + R_B}
\]

The desired voltage, 5 V, is the voltage drop, \( V_B \), across resistor \( R_B \).

\[
V_B = IR_B
\]

\( I \) is replaced by the preceding equation.

\[
V_B = IR_B = \left( \frac{V}{R_A + R_B} \right) R_B
\]

\[
V_B = \frac{V R_B}{R_A + R_B}
\]

Voltage dividers are often used with sensors such as photoresistors. The resistance of a photoresistor depends upon the amount of light that strikes it. Photoresistors are made of semiconductors such as silicon, selenium, and cadmium sulfide. A typical photoresistor can have a resistance of 400 \( \Omega \) when light strikes it, but 400 000 \( \Omega \) when in the dark. The output voltage of a voltage divider that uses a photoresistor depends upon the amount of light striking the photoresistor sensor. This circuit can be used as a light meter, such as the one in **Figure 23–5**. In this device, an electronic circuit detects the potential difference and converts it to a measurement of illuminance that can be read on the digital display.
Voltage Drops in a Series Circuit

Two resistors, 47.0-Ω and 82.0-Ω, are connected in series across a 45.0-V battery.

a. What is the current in the circuit?

b. What is the voltage drop across each resistor?

c. The 47.0-Ω resistor is replaced by a 39.0-Ω resistor. Will the current increase, decrease, or remain the same?

d. What will happen to the voltage drop across the 82.0-Ω resistor?

Sketch the Problem

- Draw a schematic of the circuit.
- Include an ammeter and voltmeters.

Calculate Your Answer

Known: Unknown:

\[ V_{\text{source}} = 45.0 \text{ V} \quad I = ? \]
\[ R_A = 47.0 \text{ Ω} \quad V_A = ? \]
\[ R_B = 82.0 \text{ Ω} \quad V_B = ? \]

Strategy:

a. To determine the current, first find the equivalent resistance.

b. Use \( V = IR \) for each resistor.

c. Calculate current again using \( R_A \) as 39.0 Ω.

d. Determine new voltage drop.

Calculations:

\[ R = R_A + R_B \]

\[ I = \frac{V_{\text{source}}}{R} = \frac{V_{\text{source}}}{R_A + R_B} \]

\[ I = \frac{45.0 \text{ V}}{47.0 \text{ Ω} + 82.0 \text{ Ω}} = 0.349 \text{ A} \]

\[ V_A = IR_A = (0.349)(47.0 \text{ Ω}) = 16.4 \text{ V} \]
\[ V_B = IR_B = (0.349)(82.0 \text{ Ω}) = 28.6 \text{ V} \]

\[ I = \frac{V_{\text{source}}}{R_A + R_B} = \frac{45.0 \text{ V}}{39.0 \text{ Ω} + 82.0 \text{ Ω}} = 0.372 \text{ A} \]

The current will increase.

\[ V_B = IR_B = (0.372)(82.0 \text{ Ω}) = 30.5 \text{ V} \]

The voltage will increase.

Check Your Answer

- Are the units correct? Current, \( A = V/\Omega \), voltage, \( V = A\Omega \).
- Is the magnitude realistic? Numerically, \( R > V \), so \( I < 1 \).

\( R \) decreases so \( I \) increases. \( V_B \) changes because it depends on \( I \).
Example Problem

Voltage Divider

A 9.0-V battery and two resistors, 400 Ω and 500 Ω, are connected as a voltage divider. What is the voltage across the 500-Ω resistor?

Sketch the Problem

• Draw the battery and resistors in a series circuit.

Calculate Your Answer

Known:

\[ V_{\text{source}} = 9.0 \text{ V} \]
\[ R_A = 400 \text{ Ω} \]
\[ R_B = 500 \text{ Ω} \]

Unknown:

\[ V_B = ? \]

Strategy:

Write the expression for the current through the circuit.

Determine equivalent resistance, \( R \).

Use voltage drop equation to determine \( V_B \).

Calculations:

\[ I = \frac{V_{\text{source}}}{R} \]

\[ R = R_A + R_B \]

\[ V_B = IR_B = \frac{(V_{\text{source}})(R_B)}{R_A + R_B} \]

\[ V_B = \frac{(9.0 \text{ V})(500 \text{ Ω})}{400 \text{ Ω} + 500 \text{ Ω}} = 5 \text{ V} \]

Check Your Answer

• Are the units correct? \( V = V \text{ Ω}/\Omega \).
• Is the magnitude realistic? The voltage drop is less than the battery voltage. Because 500 Ω is more than half of the equivalent resistance, the voltage drop is more than half the battery voltage.

Practice Problems

6. A 20.0-Ω resistor and a 30.0-Ω resistor are connected in series and placed across a 120-V potential difference.
   a. What is the equivalent resistance of the circuit?
   b. What is the current in the circuit?
   c. What is the voltage drop across each resistor?
   d. What is the voltage drop across the two resistors together?

7. Three resistors of 3.0 kΩ, 5.0 kΩ, and 4.0 kΩ are connected in series across a 12-V battery.
   a. What is the equivalent resistance?
   b. What is the current through the resistors?
   c. What is the voltage drop across each resistor?
   d. Find the total voltage drop across the three resistors.

Continued on next page

F.Y.I.

The largest voltages in your home are in your television set, where 15 000 V to 20 000 V are common. The largest currents are likely to be the 40 A in an electric range.
Parallel Circuits

Look at the circuit shown in Figure 23–6. How many current paths are there? The current from the generator can go through any of the three resistors. A circuit in which there are several current paths is called a parallel circuit. The three resistors are connected in parallel; both ends of the three paths are connected together. In the mountain river model for circuits, such a circuit is illustrated by three paths for the water over a waterfall. Some paths may have a large flow of water, others a small flow. The sum of the flows, however, is equal to the total flow of water over the falls. In addition, it doesn’t matter which channel the water flows through because the drop in height is the same. Similarly, in a parallel electrical circuit, the total current is the sum of the currents through each path, and the potential difference across each path is the same.

What is the current through each resistor? It depends upon the individual resistance. For example, in Figure 23–7, the potential difference across each resistor is 120 V. The current through a resistor is given by $I = V/R$, so you can calculate the current through the 24-Ω resistor as $I = (120 V)/(24 \, \Omega) = 5 \, A$. Calculate the currents through the other two resistors. The total current through the generator is the sum of the currents through the three paths, in this case, 38 A.

What would happen if the 6-Ω resistor were removed from the circuit? Would the current through the 24-Ω resistor change? That current depends only upon the potential difference across it and its resistance, and neither has changed, so the current is unchanged. The same is true

8. A photoresistor is used in a voltage divider as $R_B$. $V = 9.0 \, V$ and $R_A = 500 \, \Omega$.
   a. What is the output voltage, $V_{B'}$, across $R_{B'}$ when a bright light strikes the photoresistor and $R_B = 475 \, \Omega$?
   b. When the light is dim, $R_B = 4.0 \, k\Omega$. What is $V_{B'}$?
   c. When the photoresistor is in total darkness, $R_B = 0.40 \, M\Omega$ ($0.40 \times 10^6 \, \Omega$). What is $V_{B'}$?

9. A student makes a voltage divider from a 45-V battery, a 475-kΩ ($475 \times 10^3 \, \Omega$) resistor, and a 235-kΩ resistor. The output is measured across the smaller resistor. What is the voltage?

FIGURE 23–6 The parallel paths for current in this diagram are analogous to the paths that a river may take down the mountain.

FIGURE 23–7 In a parallel circuit, the reciprocal of the total resistance is equal to the sum of the reciprocals of the individual resistances.
for the current through the 9-Ω resistor. The branches of a parallel circuit are independent of each other. The total current through the generator, however, would change, and the sum of the currents in the branches would then be 18 A.

How can you find the equivalent resistance of a parallel circuit? In Figure 23–7, the total current through the generator is 38 A. A single resistor that would have a 38-A current when 120 V were placed across it would be represented by the following equation.

\[ R = \frac{V}{I} = \frac{120 \text{ V}}{38 \text{ A}} = 3.2 \Omega \]

Notice that this resistance is smaller than that of any of the three resistors in parallel. Placing two or more resistors in parallel always decreases the equivalent resistance of a circuit. The resistance decreases because each new resistor provides an additional path for current, increasing the total current while the potential difference remains unchanged.

To calculate the equivalent resistance of a parallel circuit, first note that the total current is the sum of the currents through the branches. If \( I_A, I_B, \) and \( I_C \) are the currents through the branches and \( I \) is the total current, then \( I = I_A + I_B + I_C \).

The potential difference across each resistor is the same, so the current through each resistor, for example, \( R_A \), can be found from \( I_A = \frac{V}{R_A} \). Therefore, this becomes the equation for the sum of the currents:

\[ \frac{V}{R} = \frac{V}{R_A} + \frac{V}{R_B} + \frac{V}{R_C} \]

Dividing both sides of the equation by \( V \) provides an equation for the equivalent resistance of the three parallel resistors.

**Equivalent Resistance for Resistors in Parallel**

\[ \frac{1}{R} = \frac{1}{R_A} + \frac{1}{R_B} + \frac{1}{R_C} \]

This equation can be used for any number of resistors in parallel.

### Example Problem

**Equivalent Resistance and Current in a Parallel Circuit**

Three resistors, 60.0 Ω, 30.0 Ω, and 20.0 Ω, are connected in parallel across a 90.0-V battery.

a. Find the current through each branch of the circuit.

b. Find the equivalent resistance of the circuit.

c. Find the current through the battery.

**Sketch the Problem**

- Draw a schematic of the circuit.
- Include ammeters to show the paths of the currents.
Calculate Your Answer

Known:
- \( R_A = 60.0 \, \Omega \)
- \( R_C = 20.0 \, \Omega \)
- \( R_B = 30.0 \, \Omega \)
- \( V = 90.0 \, V \)

Unknown:
- \( I_A = ? \)
- \( I_C = ? \)
- \( R = ? \)
- \( I_B = ? \)
- \( I = ? \)

Strategy:

a. The voltage across each resistor is the same, so use \( I = \frac{V}{R} \) for each branch.

b. Use the equivalent resistance equation for parallel circuits.

c. Use \( I = \frac{V}{R} \) to find the total current.

Calculations:

\[
I_A = \frac{V}{R_A} = \frac{90.0 \, V}{60.0 \, \Omega} = 1.50 \, A
\]

\[
I_B = \frac{V}{R_B} = \frac{90.0 \, V}{30.0 \, \Omega} = 3.00 \, A
\]

\[
I_C = \frac{V}{R_C} = \frac{90.0 \, V}{20.0 \, \Omega} = 4.50 \, A
\]

\[
\frac{1}{R} = \frac{1}{R_A} + \frac{1}{R_B} + \frac{1}{R_C}
\]

\[
\frac{1}{R} = \frac{1}{60.0 \, \Omega} + \frac{1}{30.0 \, \Omega} + \frac{1}{20.0 \, \Omega} = 0.100 \, \Omega^{-1}
\]

\[
R = 10.0 \, \Omega
\]

\[
I = \frac{V}{R} = \frac{90.0 \, V}{10.0 \, \Omega} = 9.00 \, A
\]

Check Your Answer

- Are your units correct? Currents are in amps, resistances are in ohms.
- Do the signs make sense? All are positive, as they should be.
- Is the magnitude realistic? \( I_A + I_B + I_C = I \)

Practice Problems

10. Three 15-\( \Omega \) resistors are connected in parallel and placed across a 30-V battery.
   a. What is the equivalent resistance of the parallel circuit?
   b. What is the current through the entire circuit?
   c. What is the current through each branch of the circuit?

11. A 120.0-\( \Omega \) resistor, a 60.0-\( \Omega \) resistor, and a 40.0-\( \Omega \) resistor are connected in parallel and placed across a 12.0-V battery.
   a. What is the equivalent resistance of the parallel circuit?
   b. What is the current through the entire circuit?
   c. What is the current through each branch of the circuit?

12. Suppose one of the 15.0-\( \Omega \) resistors in problem 10 is replaced by a 10.0-\( \Omega \) resistor.
   a. Does the equivalent resistance change? If so, how?
b. Does the amount of current through the entire circuit change? In what way?
c. Does the amount of current through the other 15.0-Ω resistors change? In what way?

Now that you have learned about both parallel and series circuits, you can analyze the brightness of the 60-W and 100-W lamps shown in the photo at the beginning of this chapter. The brightness of a lightbulb is proportional to the power dissipated by it. Used in the normal way, each bulb would be connected across 120 V. Based on what you learned in Chapter 22, the resistance of the 60-W bulb is higher than that of the 100-W bulb. But when the bulbs are connected in series, the current through the two bulbs is the same, so \( P = I^2R \). The higher-resistance lamp, the 60-W lamp, now dissipates more power and glows brighter than the 100-W lamp.

### Section Review

1. Are car headlights connected in series or parallel? Draw on your experience.

2. Lamp dimmers often contain variable resistors.
   a. Would a dimmer be hooked in series or in parallel with the lamp to be controlled? Why?
   b. Should the resistance of the dimmer be increased or decreased to dim the lamp?

3. A switch is connected in series with a 75-W bulb to a source of 120 V.
   a. What is the potential difference across the switch when it is closed or on?
   b. What is the potential difference across the switch when it is open, or off? Explain.

4. **Critical Thinking** The circuit in Figure 23–8 has four identical resistors. Suppose a wire is added to connect points A and B. Answer the following questions, explaining your reasoning.
   a. What is the current through the wire?
   b. What happens to the current through each resistor?
   c. What happens to the current drawn from the battery?
   d. What happens to the potential difference across each resistor?
You have already learned some of the elements of household wiring circuits. It’s important to understand the requirements and limitations of these systems. Above all, it is important to be aware of the safety measures that must be practiced to prevent accidents.

Safety Devices

In an electric circuit, fuses and circuit breakers are switches that act as safety devices. They prevent circuit overloads that can occur when too many appliances are turned on at the same time or a short circuit occurs in one appliance. When appliances are connected in parallel, each additional appliance placed in operation reduces the equivalent resistance in the circuit and causes more current through the wires. The additional current may produce enough thermal energy ($P = I^2R$) to melt insulation on the wires and cause a short circuit in the wires or even a fire.

A fuse is a short piece of metal that melts if too large a current passes through it. The thickness of the metal to be used is determined by the amount of current that can be safely handled by the circuit. Should there be a larger current through the circuit, the fuse will melt and break the circuit. A circuit breaker, shown in Figure 23–9, is an automatic switch that opens when the current reaches some set value. If current greater than the set value flows in the circuit, the circuit is overloaded. The circuit breaker will open and thereby stop all current.

A ground-fault interrupter is often required by law in electrical outlets in bathrooms and kitchens. Current follows a single path from the power source into the electrical outlet and back to the source. Sometimes, when an appliance such as a hair dryer is used, the appliance or user might touch a cold water pipe or a sink full of water and in this way create another current path through the user. If a current as small as 5 mA should follow this path through a person, it could result in serious injury. The ground-fault interrupter contains an electronic circuit...
that detects small differences in current caused by an extra current path and opens the circuit, thereby preventing dangerous shocks.

Electric wiring in homes uses parallel circuits, such as the one diagrammed in Figure 23–10, so that the current in any one circuit does not depend upon the current in the other circuits. The current in a device that dissipates power, $P$, when connected to a voltage source, $V$, is represented by $I = P/V$. Suppose, that in the schematic diagram shown in Figure 23–10, a 240-W television is plugged into a 120-V outlet. The current that flows is represented by $I = (240 \text{ W})/(120 \text{ V}) = 2 \text{ A}$. Then, a 720-W curling iron is plugged in. The current through the curling iron is $I = (720 \text{ W})/(120 \text{ V}) = 6 \text{ A}$. Finally, a 1440-W hair dryer is plugged in. The current through the hair dryer is $I = (1440 \text{ W})/(120 \text{ V}) = 12 \text{ A}$.

The current through these three appliances can be found by considering them as resistors in a parallel circuit in which the current through each appliance is independent of the others. The value of the resistance is found by calculating the current the appliance draws and then using the equation $R = V/I$. The equivalent resistance of the three appliances is

$$\frac{1}{R} = \frac{1}{10 \text{ } \Omega} + \frac{1}{20 \text{ } \Omega} + \frac{1}{60 \text{ } \Omega} = \frac{1}{6 \text{ } \Omega}$$

$$R = 6 \text{ } \Omega.$$  

The 15-A fuse is connected in series with the power source so the entire current passes through it. The current through the fuse is

$$I = \frac{V}{R} = \frac{120 \text{ V}}{6 \text{ } \Omega} = 20 \text{ A}.$$  

The 20-A current exceeds the rating of the 15-A fuse, so that the fuse will melt, or blow, cutting off current to the entire circuit.

A short circuit occurs when a circuit is formed that has a very low resistance. The low resistance causes the current to be very large. If there were no fuse or circuit breaker, such a large current could easily start a fire. A short circuit can occur if the insulation on a lamp cord becomes old and brittle. The two wires in the cord could accidentally touch. The resistance of the wire might be only 0.010 $\Omega$. When placed across 120 V, this resistance would result in the following current.

$$I = \frac{V}{R} = \frac{120 \text{ V}}{0.010 \text{ } \Omega} = 12 000 \text{ A}$$  

**HELP WANTED**

**ELECTRICIAN**

Electrical contractor needs electricians who have successfully completed a 5-year apprenticeship program conducted by a union or professional builder’s association. You must be a high school grad, be in good physical condition, have excellent dexterity and color vision, and be willing to work when and where there is work. You will do all aspects of the job, including reading blueprints, dealing with all types of wires, conduits, and equipment. Safety and quality work must be your highest priorities. For information contact:

International Brotherhood of Electrical Workers

1125 15th Street, N.W.

Washington, DC 20005
Such a current would cause a fuse or a circuit breaker to open the circuit immediately, thereby preventing the wires from becoming hot enough to start a fire.

**Combined Series–Parallel Circuits**

Have you ever noticed the light in your bathroom dim when you turned on a hair dryer? The light and the hair dryer were connected in parallel across 120 V. This means that the current through the lamp should not have changed when you plugged in the dryer. Yet the light dimmed, so the current must have changed. The dimming occurred because the house wiring had a small resistance in series with the parallel circuit. This is a combination series-parallel circuit. The following is a strategy for analyzing such circuits. Refer to Figure 23–1 which illustrates the procedure described in steps 1, 2, and 3 of the Problem Solving Strategy.

**Problem Solving Strategies**

**Series-Parallel Circuits**

1. Draw a schematic diagram of the circuit.
2. Find any parallel resistors. Resistors in parallel have separate current paths. They must have the same potential differences across them. Calculate the single equivalent resistance that can replace them. Draw a new schematic using that resistor.
3. Are any resistors (including the equivalent resistor) now in series? Resistors in series have one and only one current path through them. Calculate a single new equivalent resistance that can replace them. Draw a new schematic diagram using that resistor.
4. Repeat steps 2 and 3 until you can reduce the circuit to a single resistor. Find the total circuit current. Then go backwards through the circuits to find the currents through and the voltages across individual resistors.
Circuits

Problem
Suppose that three identical lamps are connected to the same power supply. Can a circuit be made such that one lamp is brighter than the others and stays on if either of the others is loosened in its socket?

Hypothesis
One lamp should be brighter than the other two and remain at the same brightness when either of the other two lamps is loosened in its socket so that it goes out.

Possible Materials
- power supply with variable voltage
- wires with clips
- 3 identical lamps and sockets

Plan the Experiment
1. Sketch a series circuit and predict the relative brightness of each lamp. Predict what would happen to the other lamps when one is loosened so that it goes out.
2. Sketch a parallel circuit and predict the relative brightness of each lamp. Predict what would happen to the other lamps when one is loosened so that it goes out.
3. Draw a combination circuit. Label the lamps A, B, and C. Would the bulbs have the same brightness? Predict what would happen to the other two lamps when each lamp in turn is loosened so that it goes out.
4. Check the Plan Show your circuits and predictions to your teacher before starting to build the circuits.
5. When you have completed the lab, dispose of or recycle appropriate materials. Put away materials that can be reused.

Analyze and Conclude
1. Interpreting Data Did the series circuit meet the requirements? Explain.
2. Interpreting Data Did the parallel circuit meet either of the requirements? Explain.
3. Formulating Hypotheses Explain the circuit that solved the problem in terms of current.
4. Formulating Hypotheses Use the definition of resistance to explain why one lamp was brighter and the other two were equally dim.
5. Making Predictions Predict how the voltages would compare when measured across each lamp in the correct circuit.
6. Testing Conclusions Use a voltmeter to check your prediction.

Apply
1. Can one wall switch control several lights in the same room? Are the lamps in parallel or series? Are the switches in parallel or series with the lamps? Explain.
**Example Problem**

**Series-Parallel Circuit**

A hair dryer with a resistance of 12.0 Ω and a lamp with a resistance of 125 Ω are connected in parallel to a 125-V source through a 1.50-Ω resistor in series.

a. Find the current through the lamp when the hair dryer is off.

b. Find the current when the hair dryer is on.

c. Explain why the lamp dims when the hair dryer is on.

**Sketch the Problem**
- Draw a diagram of the simple series circuit when the dryer is off.
- Draw the series-parallel circuit including the dryer and lamp.
- Replace \( R_A \) and \( R_B \) with a single equivalent resistance, \( R_p \).

**Calculate Your Answer**

<table>
<thead>
<tr>
<th>Known:</th>
<th>Unknown:</th>
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</thead>
<tbody>
<tr>
<td>( R_A = 125 , \Omega )</td>
<td>( I_{A1} = ? )</td>
</tr>
<tr>
<td>( R_B = 12.0 , \Omega )</td>
<td>( R = ? )</td>
</tr>
<tr>
<td>( R_C = 1.50 , \Omega )</td>
<td>( I_{A2} = ? )</td>
</tr>
<tr>
<td>( V_{source} = 125 , V )</td>
<td>( I_2 = ? )</td>
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**Strategy:**

a. When the hair dryer is off, the circuit is a simple series circuit.

b. Find the equivalent resistance for parallel circuit.

Find the equivalent resistance for entire circuit.

Use equivalent resistance to determine the current when the hair dryer is on.

c. The greater current when the hair dryer is on means a greater voltage drop across \( R_C \), which causes less voltage across \( R_A \). A decrease in voltage means current decreases, which is less power.

Current drops from 0.988 A to 0.880 A. Power, \( P = I^2R \), is smaller, consequently the light dims.
13. Two 60-Ω resistors are connected in parallel. This parallel arrangement is connected in series with a 30-Ω resistor. The combination is then placed across a 120-V battery.

a. Draw a diagram of the circuit.
b. What is the equivalent resistance of the parallel portion of the circuit?
c. What single resistance could replace the three original resistors?
d. What is the current in the circuit?
e. What is the voltage drop across the 30-Ω resistor?
f. What is the voltage drop across the parallel portion of the circuit?
g. What is the current in each branch of the parallel portion of the circuit?

Check Your Answer
- Are the units correct? Current is in amps, potential drops are in volts.
- Is the magnitude realistic? Decreased parallel resistance increases the current, causing a voltage drop in the series resistor. This leaves less voltage across the combination, so the current is smaller.

### Practice Problems

13. Two 60-Ω resistors are connected in parallel. This parallel arrangement is connected in series with a 30-Ω resistor. The combination is then placed across a 120-V battery.

a. Draw a diagram of the circuit.
b. What is the equivalent resistance of the parallel portion of the circuit?
c. What single resistance could replace the three original resistors?
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e. What is the voltage drop across the 30-Ω resistor?
f. What is the voltage drop across the parallel portion of the circuit?
g. What is the current in each branch of the parallel portion of the circuit?

### Ammeters and Voltmeters

An **ammeter** is used to measure the current in any branch or part of a circuit. If, for example, you want to measure the current through a resistor, you would place an ammeter in series with the resistor. This requires opening a current path and inserting an ammeter. The use of an ammeter should not change the current in the circuit you wish to measure. Because current would decrease if the ammeter increased the resistance in the circuit, the resistance of an ammeter should be as low as possible. **Figure 23–12** shows a real ammeter as an ideal, zero-resistance meter placed in series with a 0.01-Ω resistor. The ammeter resistance is much smaller than the values of the resistors. The current decrease would be from 1.0 A to 0.9995 A, too small to notice.

Another instrument, called a **voltmeter**, is used to measure the voltage drop across some part of a circuit. To measure the potential drop across a resistor, connect the voltmeter in parallel with the resistor. A voltmeter should have a very high resistance so that it causes the smallest possible change in currents or voltages in the circuit. Consider the circuit shown in **Figure 23–13**. A typical inexpensive voltmeter consists of an ideal, zero-resistance meter in series with a 10-kΩ resistor. When it is connected in parallel with $R_B$, the equivalent resistance of the combination is smaller than $R_B$ alone. Thus, the total resistance of the circuit decreases, increasing...
the current. \( R_A \) has not changed, but the current through it has increased, increasing the potential drop across it. The battery, however, holds the potential drop across \( R_A \) and \( R_B \) constant. Thus, the potential drop across \( R_B \) must decrease. The result of connecting a voltmeter across a resistor is to lower the potential drop across it. The higher the resistance of the voltmeter, the smaller the voltage change. Using a voltmeter with a 10 000-Ω resistance changes the voltage across \( R_B \) from 10 V to 9.9975 V, too small a change to detect. Modern electronic multimeters have even higher resistances, \( 10^7 \) Ω, and so produce even smaller changes.

### 23.2 Section Review

1. Consider the circuit in Figure 23–14 made with identical bulbs.
   a. Compare the brightness of the three bulbs.
   b. What happens to the brightness of each bulb when bulb 1 is unscrewed from its socket? What happens to the three currents?
   c. Bulb 1 is screwed in again and bulb 3 is unscrewed. What happens to the brightness of each bulb? What happens to the three currents?
   d. What happens to the brightness of each bulb if a wire is connected between points B and C?
   e. A fourth bulb is connected in parallel with bulb 3 alone. What happens to the brightness of each bulb?

2. Research and describe the connection between the physics of circuits and future careers.

3. **Critical Thinking** In the circuit in Figure 23–14, the wire at point C is broken and a small resistor is inserted in series with bulbs 2 and 3. What happens to the brightness of the two bulbs? Explain.
Electric Switch

An electric switch is a device that is used to interrupt, complete, or divert an electrical current in a circuit. Switches are found on everything from hair dryers and toaster ovens, to calculators and video games, to computers and airplane instrument panels. Some switches are simple mechanical switches. In certain devices, such as computers, however, mechanical switches are too slow and are replaced by electronic switches made from semiconducting materials.

Probably the most common type of switch is the mechanical switch you use to operate the small appliances and lights in your home or school. The switch shown below is a snap-action toggle switch typically used to turn lights off and on.

1. The insulated handle of a snap-action toggle switch can be flipped in either of two positions—off or on.

2. When the handle is in the off position, as it is in this diagram, metal contacts within the switch are separated, interrupting the path of the current.

3. When the handle is in the on position, the metal contacts, which are linked by wires, come together to complete the circuit.

4. One wire leads to a grounding location. Then if a problem occurs with the wires or switch contacts, the current is routed to the ground, not to the person touching the switch.

5. The switch casing is insulated, so if a wire becomes loose or frayed and touches the casing, current will not flow.

Thinking Critically

1. Circuit breakers are automatic switches. Explain why this is so.

2. Why must the contacts in a switch be metal? Why are switch handles often plastic?
CHAPTER 23 REVIEW

Summary

**23.1 Simple Circuits**
- The current is the same everywhere in a simple series circuit.
- The equivalent resistance of a series circuit is the sum of the resistances of its parts.
- The sum of the voltage drops across resistors in series is equal to the potential difference applied across the combination.
- A voltage divider is a series circuit used to produce a voltage source from a higher-voltage battery.
- The voltage drops across all branches of a parallel circuit are the same.
- In a parallel circuit, the total current is equal to the sum of the currents in the branches.
- The reciprocal of the equivalent resistance of parallel resistors is equal to the sum of the reciprocals of the individual resistances.
- If any branch of a parallel circuit is opened, there is no current in that branch. The current in the other branches is unchanged.

**23.2 Applications of Circuits**
- A fuse or circuit breaker, placed in series with appliances, creates an open circuit when dangerously high currents flow.
- A complex circuit is often a combination of series and parallel branches. Any parallel branch is first reduced to a single equivalent resistance. Then any resistors in series are replaced by a single resistance.
- An ammeter is used to measure the current in a branch or part of a circuit. An ammeter always has a low resistance and is connected in series.
- A voltmeter measures the potential difference (voltage) across any part or combination of parts of a circuit. A voltmeter always has a high resistance and is connected in parallel with the part of the circuit being measured.

**Key Terms**

23.1
- series circuit
- equivalent resistance
- voltage divider
- parallel circuit

23.2
- fuse
- circuit breaker
- ground-fault interrupter
- short circuit
- combination series-parallel circuit
- ammeter
- voltmeter

**Key Equations**

**23.1**

\[ R = R_A + R_B + \ldots \quad I = \frac{V_{\text{source}}}{R} \quad \frac{1}{R} = \frac{1}{R_A} + \frac{1}{R_B} + \frac{1}{R_C} \]

**Reviewing Concepts**

**Section 23.1**

1. Why is it frustrating when one bulb burns out on a string of holiday tree lights connected in series?
2. Why does the equivalent resistance decrease as more resistors are added to a parallel circuit?
3. Several resistors with different values are connected in parallel. How do the values of the individual resistors compare with the equivalent resistance?
4. Why is household wiring done in parallel instead of in series?
5. Why is there a difference in total resistance between three 60-Ω resistors connected in series and three 60-Ω resistors connected in parallel?
6. Compare the amount of current entering a junction in a parallel circuit with that leaving the junction. *Note:* A junction is a point where three or more conductors are joined.

**Section 23.2**

7. Explain the function of a fuse in an electric circuit.
8. What is a short circuit? Why is a short circuit dangerous?
9. Why does an ammeter have a very low resistance?
10. Why does a voltmeter have a very high resistance?
11. How does the way in which an ammeter is connected in a circuit differ from the way a voltmeter is connected?

**Applying Concepts**

12. What happens to the current in the other two lamps if one lamp in a three-lamp series circuit burns out?
13. Suppose that in the voltage divider in Figure 23–4, the resistor $R_A$ is made to be a variable resistor. What happens to the voltage output, $V_B$, of the voltage divider if the resistance of the variable resistor is increased?
14. Circuit A contains three 60-$\Omega$ resistors in series. Circuit B contains three 60-$\Omega$ resistors in parallel. How does the current in the second 60-$\Omega$ resistor change if a switch cuts off the current to the first 60-$\Omega$ resistor in
   a. circuit A?
   b. circuit B?
15. What happens to the current in the other two lamps if one lamp in a three-lamp parallel circuit burns out?
16. An engineer needs a 10-$\Omega$ resistor and a 15-$\Omega$ resistor. But there are only 30-$\Omega$ resistors in stock. Must new resistors be purchased? Explain.
17. If you have a 6-V battery and many 1.5-V bulbs, how could you connect them so that they light but do not have more than 1.5 V across each bulb?
18. Two lamps have different resistances, one larger than the other.
19. For each of the following, write the form of circuit that applies: series or parallel.
   a. The current is the same throughout.
   b. The total resistance is equal to the sum of the individual resistances.
   c. The voltage drop is the same across each resistor.
   d. The voltage drop is proportional to the resistance.
   e. Adding a resistor decreases the total resistance.
   f. Adding a resistor increases the total resistance.
   g. If the current through one resistor goes to zero, there is no current in the entire circuit.
   h. If the current through one resistor goes to zero, the current through all other resistors remains the same.
   i. This form is suitable for house wiring.
20. Why is it dangerous to replace a 15-A fuse in a circuit with a fuse of 30 A?

**Problems**

**Section 23.1**

21. A 20.0-$\Omega$ lamp and a 5.0-$\Omega$ lamp are connected in series and placed across a potential difference of 50.0 V. What is
   a. the equivalent resistance of the circuit?
   b. the current in the circuit?
   c. the voltage drop across each lamp?
   d. the power dissipated in each lamp?
22. The load across a battery consists of two resistors, with values of 15 $\Omega$ and 45 $\Omega$, connected in series.
   a. What is the total resistance of the load?
   b. What is the voltage of the battery if the current in the circuit is 0.10 A?
23. A lamp having a resistance of 10.0 $\Omega$ is connected across a 15-V battery.
   a. What is the current through the lamp?
   b. What resistance must be connected in series with the lamp to reduce the current to 0.50 A?
24. A string of 18 identical holiday tree lights is connected in series to a 120-V source. The string dissipates 64.0 W.
   a. What is the equivalent resistance of the light string?
   b. What is the resistance of a single light?
   c. What power is dissipated by each lamp?

25. One of the bulbs in problem 24 burns out. The lamp has a wire that shorts out the lamp filament when it burns out. This drops the resistance of the lamp to zero.
   a. What is the resistance of the light string now?
   b. Find the power dissipated by the string.
   c. Did the power go up or down when a bulb burned out?

26. A 75.0-W bulb is connected to a 120-V source.
   a. What is the current through the bulb?
   b. What is the resistance of the bulb?
   c. A lamp dimmer puts a resistance in series with the bulb. What resistance would be needed to reduce the current to 0.300 A?

27. In problem 26, you found the resistance of a lamp and a dimmer resistor.
   a. Assuming that the resistances are constant, find the voltage drops across the lamp and the resistor.
   b. Find the power dissipated by the lamp.
   c. Find the power dissipated by the dimmer resistor.

28. A 16.0-Ω and a 20.0-Ω resistor are connected in parallel. A difference in potential of 40.0 V is applied to the combination.
   a. Compute the equivalent resistance of the parallel circuit.
   b. What is the current in the circuit?
   c. How large is the current through the 16.0-Ω resistor?

29. Amy needs 5.0 V for some integrated circuit experiments. She uses a 6.0-V battery and two resistors to make a voltage divider. One resistor is 330 Ω. She decides to make the other resistor smaller. What value should it have?

30. Pete is designing a voltage divider using a 12.0-V battery and a 100.0-Ω resistor as $R_B$. What resistor should be used as $R_A$ if the output voltage across $R_B$ is to be 4.00 V?

31. A typical television dissipates 275 W when it is plugged into a 120-V outlet.

   a. Find the resistance of the television.
   b. The television and 2.5-Ω wires connecting the outlet to the fuse form a series circuit that works like a voltage divider. Find the voltage drop across the television.
   c. A 12-Ω hair dryer is plugged into the same outlet. Find the equivalent resistance of the two appliances.
   d. Find the voltage drop across the television and hair dryer. The lower voltage explains why the television picture sometimes shrinks when another appliance is turned on.

Section 23.2

32. A circuit contains six 240-Ω lamps (60-W bulbs) and a 10.0-Ω heater connected in parallel. The voltage across the circuit is 120 V. What is the current in the circuit
   a. when four lamps are turned on?
   b. when all lamps are on?
   c. when six lamps and the heater are operating?

33. If the circuit in problem 32 has a fuse rated at 12 A, will the fuse melt if everything is on?

34. Determine the reading of each ammeter and each voltmeter in Figure 23–15.

35. Determine the power used by each resistance shown in Figure 23–15.

36. During a laboratory exercise, you are supplied with a battery of potential difference $V$, two heating elements of low resistance that can be placed in water, an ammeter of very small resistance, a voltmeter of extremely high resistance, wires of negligible resistance, a beaker that is well insulated and has negligible heat capacity, and 100.0 g of water at 25°C.
   a. By means of a diagram and standard symbols, show how these components should be connected to heat the water as rapidly as possible.
b. If the voltmeter reading holds steady at 50.0 V and the ammeter reading holds steady at 5.0 A, estimate the time in seconds required to completely vaporize the water in the beaker. Use 4200 J/kg·°C as the specific heat of water and 2.3 × 10^6 J/kg as the heat of vaporization of water.

37. A typical home circuit is shown in Figure 23–16. The lead lines to the kitchen lamp each has a very low resistance of 0.25 Ω. The lamp has a resistance of 240.0 Ω. Although it is a parallel circuit, the lead lines are in series with each of the components of the circuit.

![Figure 23–16](image)

a. Compute the equivalent resistance of the circuit consisting of just the light and the lead lines to and from the light.
b. Find the current to the bulb.
c. Find the power dissipated in the bulb.

38. A power saw is operated by an electric motor. When electric motors are first turned on, they have a very low resistance. Suppose that a kitchen light in problem 37 is on and a power saw is turned on. The saw and lead lines have an initial total resistance of 6.0 Ω.

b. What is the total current flowing in the circuit?
c. What is the total voltage drop across the two leads to the light?
d. What voltage remains to operate the light? Will this cause the light to dim temporarily?

**Critical Thinking Problems**

39. A 50-200-250-W three-way bulb has three terminals on its base. Sketch how these terminals could be connected inside the bulb to provide the three brightnesses. Explain how to connect 120 V across two terminals at a time to obtain a low, medium, and high level of brightness.

40. Batteries consist of an ideal source of potential difference in series with a small resistance. The electrical energy of the battery is produced by chemical reactions that occur in the battery. However, these reactions also result in a small resistance that, unfortunately, cannot be completely eliminated. A flashlight contains two batteries in series. Each has a potential difference of 1.50 V and an internal resistance of 0.200 Ω. The bulb has a resistance of 22.0 Ω.

a. What is the current through the bulb?
b. How much power does the bulb dissipate?
c. How much greater would the power be if the batteries had no internal resistance?

**Going Further**

**Using What You’ve Learned** An ohmmeter is made by connecting a 6.0-V battery in series with an adjustable resistor and an ideal ammeter. The ammeter deflects full-scale with a current of 1.0 mA. The two leads are touched together and the resistance is adjusted so that 1.0 mA flows.

a. What is the resistance of the adjustable resistor?
b. The leads are now connected to an unknown resistance. What resistance would produce a current of half-scale, 0.50 mA?
c. What resistance would produce a reading of quarter-scale, 0.25 mA?
d. What resistance would produce a reading of three-quarters-scale, 0.75 mA?